

Peter Grünwald, Petri Myllymäki, Ioan Tabus, Marcelo Weinberger & Bin Yu (eds.)

Festschrift in Honor of Jorma Rissanen on the Occasion of his 75th Birthday



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Peter Grünwald, Petri Myllymäki, Ioan Tabus, Marcelo Weinberger & Bin Yu (eds.)

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Preface

This *Festschrift* is presented in honor of Jorma Rissanen, on the occasion of his 75th birthday on October 20th, 2007. It contains 20 contributions by Jorma's colleagues and friends covering a wide range of topics in the areas of information theory, statistical modeling and inference, data compression and applications of modeling in science, engineering, and economics, reflecting the many areas where Jorma's work had a great impact.

A special session will be organized in the IEEE Information Theory Workshop to be held in Porto, Portugal during May 5-9, 2008. A number of the contributions will be presented in the special session of the workshop and the final printed copy of the edited version of the present volume will be available.

Jorma's exemplary career and his discoveries are a continuous source of inspiration for generations of researchers and students. His discoveries in science have had a substantial impact on the foundations of statistics and information theory. They prove fruitful in a wide range of applications, including science (psychology, molecular biology, astrophysics), engineering (control, computer science, signal processing), and economics.

Jorma is energetic as ever, constantly producing novel, galvanizing contributions in his positions as professor emeritus at Tampere University of Technology, visiting professor at Helsinki University of Technology and University of London, and HIIT Fellow at Helsinki Institute for Information Technology.

This volume is built out of contributions continuing in many ways the line of thoughts and principles promoted by Jorma, giving a glimpse of the diversity of areas relevant to his research. This volume will also reveal some insights of his remarkable personal life. All those who have had the privilege to meet and work with him have been amazed to see in him such an example of staying straight in life and being faithful to his pursuit of truth and values through science.

We wish to Jorma the fulfillment of all his wishes and strength to continue transforming his wishes into reality.

Happy Birthday!

Bin, Ioan, Marcelo, Peter, and Petri

Berkely, Tampere, Palo Alto, Amsterdam, Helsinki

October 20th, 2007

A Conversation with Jorma Rissanen

Pentti Huuhtanen, Erkki P. Liski and Simo Puntanen

Brief Biography

Jorma Johannes Rissanen was born in Pielisjärvi, Finland, on October 20, 1932. He received his Master's degree in electrical engineering in 1956, his Licentiate and Doctor of Technology degrees in control theory and mathematics in 1960 and 1965, respectively, all from the Helsinki University of Technology, Finland. He joined IBM's San Jose Research Laboratory, California, 1966, where he remained for more than three decades, except for the academic year 1973–74, when he held the chair of control theory in Linköping University, Sweden. He is a fellow of the Helsinki Institute for Information Technology, University of Helsinki. He is also a Professor Emeritus at the Tampere University of Technology. Since 1998 he has been appointed Visiting Professor in Computer Science at Royal Holloway, University of London. He is a Foreign Member of the Finnish Academy of Science and Letters and he has received an Honorary Doctorate degree from the Tampere University of Technology, Finland, in 1992.

Jorma Rissanen is the founder of the Minimum Description Length (MDL) principle, a new inductive principle in statistical modeling. He has carried out significant research in the fields of control, prediction and system theories, relation theory, numerical mathematics, information and coding theory, probability theory and statistics. He has published more than a hundred research papers and the books *Stochastic Complexity in Statistical Inquiry* (1989, World Scientific) and *Information and Complexity in Statistical Modeling* (2007, Springer), and he holds 15 US patents. He continues to be active in research.

Jorma Rissanen has earned many honors and awards, including the 2006 Kolmogorov Medal of the Computer Learning Research Centre at Royal Holloway, University of London; an IEEE Information Society Golden Jubilee Award for Technological Innovation for the invention of arithmetic coding in 1998; the IEEE 1993 Richard W. Hamming medal 'For fundamental contributions to information theory, statistical inference, control theory, and the theory of complexity'; an IBM Corporate Award in 1991 for the MDL/PMDL principles and stochastic complexity; an IBM Outstanding Innovation Award in 1988 for work in statistical inference, information theory, and the theory of complexity; the Best Paper Award from the IEEE Information Theory Group in 1986 (covered all papers published in information theory during the preceding two-year period); the Best Paper Award from the International Federation of Automatic Control in 1981; an IBM Outstanding Innovation Award in 1980 for the introduction of arithmetic codes. He is an IEEE Fellow.

In 1956 he married Riitta Åberg, and they have a son Juhani and a daughter Natasha, one grandson Juhani and one granddaughter Elissa.

The following conversation took place both by email in the end of July and meeting in Tampere in August 2007.

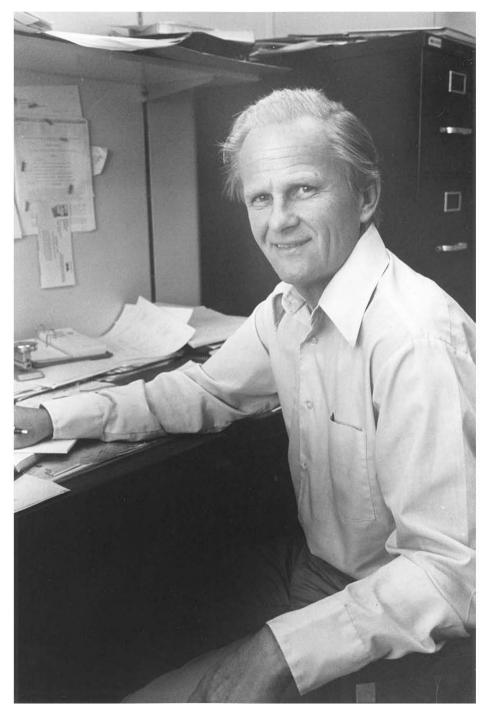


Figure 1: Jorma Rissanen in his San Jose office in 1985.

Early life, Kemi, wartime, 1932–55

QUESTION: Jorma, let us start at the very beginning. You were born on October 20, 1932 in Pielisjärvi, near then the Soviet border, but soon your family moved to Kemi, which is situated in the north-western part of Finland near to the Sweden-Finland border. Jorma, tell us something about your family and your childhood in Kemi.

JORMA RISSANEN: There isn't all that much to tell. We lived in rented apartments in various suburbs of the small town, and just about all I remember of the period before the war was that it was cold and there were huge piles of snow.

Did you have sisters or brothers?

I had four sisters and a brother.

Soon after you went to primary school in 1939 the Winter War broke out when the Soviet Union attacked Finland on November 30, 1939. The war lasted 100 days. What kind of time was that in your life?

It did not affect us too much. Since Kemi is hundreds of kilometers from the Soviet border we had no bombing, even though we had to go to bomb shelters a few times.

The period of peace after the Winter War was short. The Continuation War lasted from June 25, 1941 until September 19, 1944. Germany took part by providing critical material support and military cooperation to Finland and also some German troops operated in North Finland. When Finland in September 1944 made peace with the Soviet Union the so-called Lapland War broke out between Finland and Germany. Your home town Kemi was also in the middle of battles. Could you tell about your personal war experiences?

Just before the fighting reached the house where we lived we took off to the woods together with the family of the owner of the house, a horse and a cow. There we waited for a few days until fighting passed the area. When the sound of the cannon shots seemed to come from farther away I decided to take a look at our home on the main road to north. A miles long German column of vehicles of any sort had been stopped on the road with dead soldiers with their arms lying nearby. I, together with the neighborhood boys, had a keen interest in guns and ammunition, and I thought that this is an excellent opportunity to get Schmeisser machine pistols. I picked two and hid them under the house where we lived. Every room of the apartment had bullet holes so that none of us would have survived if we had stayed. On the yard behind an Y-shape tree a dead German soldier with his machine rifle was lying. I was tempted to take the rifle but it was too long and heavy and I left it. Unfortunately I had no chance to try the machine pistols, because the next few days a Finnish soldier came to check if there are any weapons around, and my father told him that I had a cache under the house. I remember those as exciting times!

How about your early schooling in wartime?

After the Germans were pushed to Norway there was almost nothing to eat in Kemi, and I was sent with many others to Sweden, where I stayed one year without attending any school and missed the third grade. I learned Swedish though, which I however kept forgetting faster than what I was taught an hour every day from the third grade on in the junior high school.



Figure 2: Conference in Ann Arbor, Michigan: Jorma Rissanen and Claude Shannon. Jorma Rissanen has received the Best Paper Award from IEEE Information Theory Group in 1986.

What can you recall about your life during the elementary, junior high and high school days? Did you start showing any added aptitude in one subject over others at some stage?

For a couple of years I had trouble with arithmetic and mathematics, but then all of a sudden, it seemed, I understood that arithmetic and mathematics is nothing but a game with certain rules, which you have to learn. After that it became my favorite field.

Our mathematics teacher happened to be excellent. He kept on reminding the students that there is nothing to learning mathematics and all of you are capable of getting at least the grade B. He left me with the long lasting impression that I should be able to learn anything if it is explained clearly.

Of science we were taught basic physics, the teacher of which was very good, too.

How about the matriculation examination in the early 1950s? What kind of thoughts does that bring to your mind?

The examination itself took one whole day. I remember the 3-hour mathematics test, which consisted of ten problems. One was an involved percentage type of problem, which was very hard

to decipher, and I missed it. However, since it was the only one I missed I still got the grade 'laudatur' and was allowed to attend the 2-week summer school for the Technical University of Helsinki. The other tests meant nothing to me and I must have passed them because I graduated.

Helsinki University of Technology, 1952–56

You enrolled in the undergraduate programme at Helsinki University of Technology (HUT) in 1952. How did you become interested in engineering studies?

At the time there were two favorite ways to proceed towards higher education with good career prospects, the medical and technical fields, and my choice was clear: the most prestigious technical university of Finland was in Helsinki.

After the years in Kemi, how did you like to live in Helsinki in your student years?

I actually lived in Helsinki itself only the first year, after which I moved to Otaniemi and took the bus to the old technical university building, where all the lectures were given. I had no social life other than soccer, which we played just about every night in the newly built indoors arena in Otaniemi.

Do you recall teachers or other people at HUT that you regard as influences on your career as it developed?

Hans Blomberg, the professor of theoretical electrical engineering was excellent. So was the mathematics professor Kalle Väisälä, from whom I took all the courses he gave.

You served in the army right after finishing the undergraduate degree in 1956. How did you cope with the mandatory military assignment?

My military career ended prematurely when I hurt my knee and was operated, which gave me a good chance to study for the Licentiate degree in the military hospital.

I recall that this knee problem has not been entirely solved and it has not allowed you to play soccer according to your talents? Is that right?

That is right. I didn't play soccer in the following ten years until a knee specialist in California told me that there is nothing much wrong with the knee and go ahead and start playing, which I did.

You started your Licentiate studies in 1957. What form were these studies? Was your aim already directed at a doctoral degree?

There were no courses on control theory, and I picked the topic for graduate studies because of Hans Blomberg's interest in it. My aim certainly was a doctoral degree.

You have told that one of your first places of employment was the Helsinki City Utility Company.

It was my first steady employment; after all, I had just married and had to make a living.



Figure 3: Conference Dinner in Tampere Conference 1987: T. W. Anderson, Jorma Rissanen and Dorothy Anderson.

So you were working and continuing your studies at the same time?

Yes.

When did your interests in mathematics and science begin to emerge?

They grew gradually during the undergraduate studies.

What was your dissertation about?

It was about the horrible problem of adaptive control.

Could you please be a bit more specific? Your answers makes me curious...

Although I feel the less said about the thesis the better, let me just add that the most important and difficult part in problem selection is to pick a topic which both is tractable and reasonably significant. Since nobody had been able to do anything worthwhile about the adaptive control problem I should never have taken that as a PhD topic. Needless to say I wasted my time as well as that of the examiner, Olli Lokki, and produced absolutely nothing worthwhile.

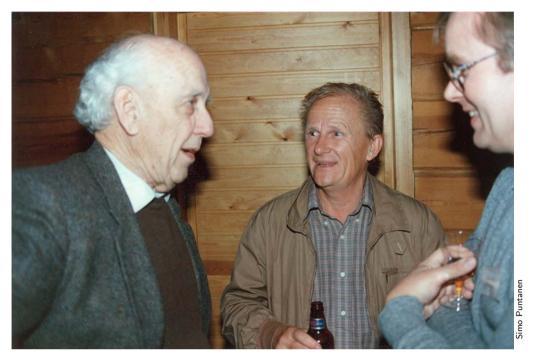


Figure 4: Sauna Party in Tampere Conference 1987: Ted Hannan, Jorma Rissanen, and Heikki Hella.

Who was your thesis advisor and what kind of process it was to work for a doctoral degree at that time at HUT?

My thesis advisor was Hans Blomberg, and since there were no formal lectures given on graduate level I simply started by reading literature given to me by him. I continued studying mathematics under the tutoring of Kalle Väisälä. The examination was done in my working out problems in books as home work – not avoiding the more difficult ones as instructed by Professor Väisälä.

Often, work done for doctoral thesis shapes one's future conception of the field. Is this the case for you?

No.

Are there other people at HUT that you regard as influences on your career as it developed?

No.

You received the Doctor of Technology Degree in control theory and mathematics from the Helsinki University of Technology in 1965. Were there many other doctoral students in your field of research at HUT?

Since I did most of my work away from the university while working for IBM, I didn't know of any other doctoral student in any field at HUT.

Did you have any contacts with the Department of Mathematics at the University of Helsinki? At that time there were many world famous mathematicians like e.g. Rolf Nevanlinna, Paul Kustaanheimo, P. J. Myrberg, Gustav Elfving and Olli Lehto.

I had no contact with the Department of Mathematics at the University of Helsinki, but I did know the impressive Paul Kustaanheimo and of course I knew Olli Lokki who was at the HUT. In fact, my first course in statistics were lectures given at HUT by Olli Lokki, who was the pioneer of statistics teaching in HUT.

What were your plans for future after finishing your degree? How did you originally get interested in research career?

It seems now that I have always regarded research as the only career for me, which was only strengthened while working in IBM Research.

What about the teaching? Did you feel any call for teaching after finishing your degree?

I didn't have a chance until later when I found out that teaching is too difficult to be left to the professionals.

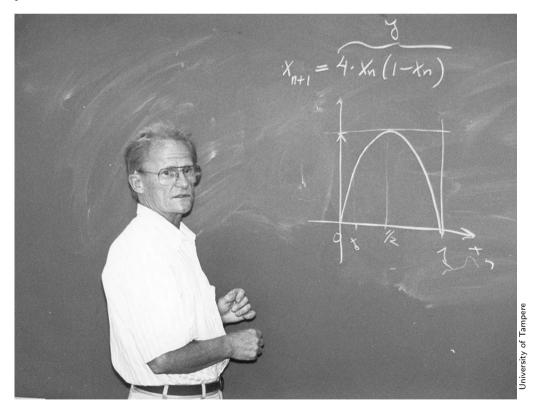


Figure 5: Workshop in Tampere 1990. Jorma Rissanen talking on "Stochastic Complexity in Linear Models".

Sweden, 1958–64

You started your international career in Sweden in 1958. You worked at ASEA in Västerås? Could you tell something about that time?

I was told at the Helsinki City Utility Company that "by law we cannot fire you because of the military service, but don't come back". I never did. In fact I left the whole country and joined ASEA. I formulated and proved my very first theorem, one of the fundamental theorems in control (Rissanen 1961). It states that by a linear feedback you can move the poles wherever you wish but you cannot change their number.

You moved to the IBM Nordic Laboratory in Stockholm in 1960.

Yes, I did, and was sent for one year visit to Yorktown Heights and San Jose. These visits turned out to be crucial for my entire future.

Information technology and industry lived their early stages in these times. Do you find that this has some effect on your orientation in research?

The mission of the IBM Nordic Laboratories was industrial process control, but after a few years the company grew tired of waiting for economic results from that. The main problem was not control, which was easy if you knew what you were supposed to control. This turned my interests to modeling, and as it happens I never got out of it. The effect of information technology to my career was still some years away – and in fact came from an unexpected direction. But more of that a bit later.

Your first published works were on linear systems and prediction theory. Are we right?

Yes, I mentioned above my very first pole shifting theorem for linear feedback systems. In addition in the mid sixties I derived fast algorithms for factoring Hankel and Toeplitz matrices, which solve the so-called system identification problem as well as the Kalman type of prediction problem for ARMA processes (Rissanen 1973).

To the USA and to IBM, 1964–

You left Stockholm in 1964 and moved to the States. First to Electronic Associates in Princeton and Lockheed in Huntsville, but soon back to IBM's San Jose Research Laboratory, California. That was a time of many changes of residence. Tell us what made you to get off the ground.

Well, I needed a sponsor in the USA for emigration, and my boss in IBM USA during the visit had been promoted, which left me without a contact. I thought that who needs IBM and joined Electronic Associates. I realized however that maybe I had made a mistake and when IBM showed interest in getting us to San Jose we were just too happy to comply.

Did you join a research group in San Jose or did you work more or less independently? Tell us about the research culture and atmosphere at IBM.

I joined a research group but was given quite free hands to study and work on my own problems. This I took advantage of and became a professional student.

San Jose is geographically pretty close to some of America's greatest universities. Did you develop connections with people in Stanford and Berkeley?

Yes, indeed. I gave graduate lectures in Berkeley on prediction theory, and visited regularly professors Rudy Kalman and Tom Kailath in Stanford University. Later I actually was an adjunct professor in Stanford University.

What kind of working habits did you follow? How would you describe a normal day?

I started at about 8 AM and studied or worked on a problem leading to a paper until 5 PM. It took many years to get accustomed to such a regime without any obligations or directions – just study without focus and search for a meaningful problem. Every other day at noon time I played pickup soccer, which was a great distraction and broke the monotonous day.

In 1973-74 you held the chair of control theory in Linköping University, Sweden. It was not your cup of tea?

Immigrants often tend to feel nostalgia after a few years, and this happened to us as well. Also the lack of focus in my research had an effect, and when I saw the advertizement of a professor chair in Sweden I thought why not. It was a disastrous move. I found out that I don't like the field of control, I don't like to be a professor, and I don't like the climate nor the at that time socialistic Sweden. However, something happened, which maybe could not have happened otherwise. I was exposed to the exciting ideas of Chaitin, Kolmogorov, and Martin-Löf, which set my mind in fire. I found that this is what interests me, and finally I could focus on something that also could be of some interest to IBM. We returned to San Jose after just one year.

Did you have any personal contact with Kolmogorov?

I never had the honor of meeting him.

Did you meet Harald Cramér while you were in Sweden?

No, I never met him. But if you were to ask my statistical idols, I would definitely mention Harald Cramér and R. A. Fisher.

Arithmetic coding, stochastic complexity and MDL, 1975–

Many works you did at that time were somehow related to time series analysis. The Box-Jenkins approach to modeling ARIMA processes was described in a highly influential book by statisticians George Box and Gwilym Jenkins in 1970 (Box and Jenkins 1970). It seems that you already were familiar with these kinds of techniques at that time. Was it because of your system and prediction theory background?

Yes indeed. The modeling problems for AR and ARMA processes were bread and butter in the control field a decade before the Box–Jenkins book.

Later you had joint works with Ted Hannan who was one of the foremost experts in time series analysis. Would you like to say something about your collaborations with him?

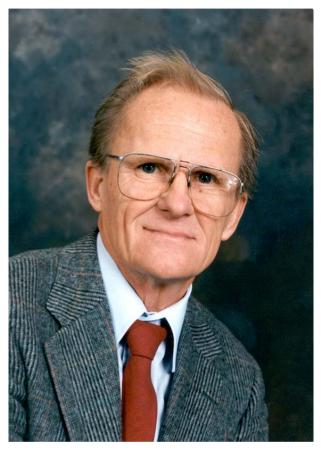


Figure 6: The IEEE announced that Jorma Rissanen is the recipient of the 1993 IEEE Richard W. Hamming Medal (IEEE Information Theory Society Newsletter 1993).

Ted loved to work on the difficult analysis problems arising in time series. His forte was analysis of existing problems rather than the creation of new ones. Among his many results was to derive a rather exact form for the penalty term in a criterion to find the number of parameters consistently. This also implies the consistency of the criterion BIC or the asymptotic approximation of the MDL criterion. To show something of my two-month visit to the Australian National University we had a joint *Biometrika* paper, written mostly by him, on estimation of ARMA order (Hannan and Rissanen 1982).

In 1975 you introduced a new coding technique for data compression, called Arithmetic Coding, which is certainly one of your main contributions (Rissanen 1976). We may guess that coding theory was not one of your study subjects in the Helsinki University of Technology. Was it at IBM when you became interested in coding theory?

I had never heard of the coding problem at the time I stayed at HUT. I got the idea of arithmetic coding from the brief paper by Kolmogorov, 'Three Measures of Information' (Kolmogorov 1965), during my stay as the professor of control theory in Sweden.

How do you see the status of Arithmetic Coding nowadays?

It is very simply the preferred way of doing coding for data compression. It has relegated the optimal, elegant, and then dominant Huffman codes to a graceful retirement – as someone put it.

You introduced in 1983 a universal modeling algorithm Context, called now variable order Markov chains (Rissanen 1983). Tell us about the research that led to Context.

I got the idea from the elegant data compression algorithm by Lempel and Ziv. Since I was advocating the view that all universal data compression algorithms must incorporate a model of the data, I first reinterpreted the main part in the LZ algorithm as a universal model in the huge class of ergodic processes. This then led to the universal modeling algorithm Context for the much smaller class of Markov chains. Because the class is smaller the model cost is smaller too, and you get a better compression if the data have any properties like the Markov chains.

Many people would like to know what led you into formulating the principle that is now known as the MDL principle?

Since with arithmetic coding you can encode any data modeled in any statistical manner in a completely mechanical and uniform way the key problem in data compression is to understand the statistical behavior of the data, which is modeling. I then turned the problem around and concluded that it is possible to measure the goodness of any model by its ability to compress the data. This relationship becomes evident by Kraft inequality, which establishes the logical equivalence between a distribution and the lengths of a (prefix) code tree.

Was the MDL principle formulated the first time in your Automatica paper "Modeling by shortest data description" in 1978, or even before?

Yes. The MDL principle as a concept was clear to me after the introduction of arithmetic coding in around 1975–1976, and in the *Automatica* paper I wanted to explain the principle to an audience not familiar with coding but one which I was familiar with, the control theory people.

You were inspired by the Kolmogorov's algorithmic theory of complexity. There are also the related works by Ray Solomonoff, G. J. Chaitin and Per Martin-Löf. Do you think that their works had some influence on your thinking?

In a fundamental way. You see, it is one thing to understand things intuitively but quite different to see formally the relationships, which is what I learned from the writings of these distinguished men. In fact, there are still certain baffling both conceptual and technical issues, which I hope to be able to sort out some day.

The idea of estimation-via-coding was presented in the computer science literature by Wallace and Boulton 1968. How is their approach related to MDL?

First, their principle is expressed as minimizing the mean code length, which is then estimated. This results in a two-part code, which Wallace and his students have applied to a number of practical cases. The MDL principle on the other hand has been developed into a theory of inference rather than just a criterion for model selection.

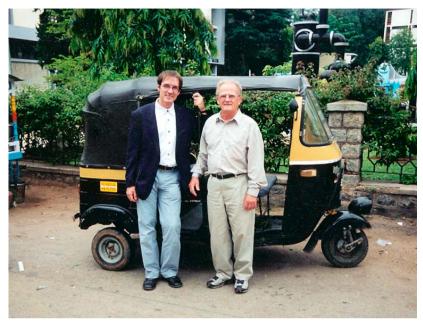


Figure 7: Peter Grünwald and Jorma Rissanen during the 2002 IEEE Information Theory Workshop in Bangalore, India.

Your paper 'Stochastic complexity and modeling' in Annals of Statistics 1986 extends certain fundamental results in information theory and statistics. Could you tell us in a few words about the significance of this contribution.

At the time I wanted to prove that with a parametric family of distributions you cannot get a shorter code length for or, equivalently, a greater probability assigned to data sequences than a certain calculable bound – no matter how you construct the code. That is, such a bound, which I called stochastic complexity, is inherent for the family of distributions at hand. Later constructions were found with which the bound can be essentially achieved. This simply means that there are some absolute restrictions in modeling which you have to live with, and if your model gets away with such restrictions nobody can beat you. This is the aim with universal models.

During the last three decades you have developed such ideas as stochastic complexity, universal model, and universal minimal sufficient statistics, which provide an information theoretic foundation for statistics. How do you assess the present status of your theory now?

The universal minimal sufficient statistics in the algorithmic information theory, where a model of data is simply any finite set that includes the data, is due to Kolmogorov. When we deal with distributions as models, which must be estimated from data, there is a possibility to sharpen Kolmogorov's result at least in two respects: First, the code length of a model, represented by the maximum likelihood estimate of its parameters, corresponds to the Kolmogorov complexity of the model. But the model can actually be represented more completely by the sequence of the maximum likelihood estimates, obtained from all the prefixes of the data sequence. This has no

counter part in the algorithmic theory, and clearly there is more information about the model in the sequence of the maximum likelihood estimates than in just the last estimate. Hence, the idea of 'information' that an estimated model represents is now different and more complex.

The second aspect which is missing in the algorithmic models is the idea of models that can be optimally 'distinguished' from a given set of data. I have written about how this provides a sense of optimality in hypothesis testing and greatly reduces the number of hypotheses we need to test.

My most recent work is of a new generation of universal models, which, while related to the predictive ways of constructing universal models like Dawid's prequential 'plug-in' models or the equivalent predictive MDL models, are strictly better – provably so.

If you were asked to list your three most important contributions, what would you list?

The two most important contributions are undoubtedly Arithmetic Coding and the MDL principle. The third is tougher to pick. The theorem on the lower bound for the code length achievable for parametric families mentioned above together with the latest extensions of the MDL theory rank in my mind higher than Algorithm Context – perhaps because of the much greater difficulty in deriving them. In fact, I understand the proof in the *Annals of Statistics* paper only in my brighter moments.

Philosophy

In research, which is more important: conceptual foundations or technical perfection?

I think the conceptual foundations are more important although their clarifications require often difficult analysis, which, moreover, tends to modify the initial concepts, and hence we cannot really separate the two.

Do you see the computer as a tool in theoretical work?

Computations of anything I have proposed have influenced my theoretical work (shown that I had overlooked something).

What is your approach to a problem? Do you have certain techniques or would you say that is intuitive?

My intuition amounts to seeing, or better feeling, what's essential in the problem. Then by analysis comes a sharper isolation of that essential, which amounts to better understanding of the problem. The rest is detail – albeit sometimes crucial detail. An example is coding, in which the essential is just sorting and counting. However, the crucial thing is to understand exactly what it is that should be counted. In fact, this is also behind the entropy and the algorithmic information, so that in essence Kolmogorov's three measures of information could be reduced to one. Clearly, to find the essence can be difficult, although in case of arithmetic coding it was not difficult, because of Kolmogorov's paper, where the essence was spelled out. Nevertheless, after the invention of arithmetic codes my boss cum secretary exclaimed that he could not have invented that in a million years, or, more realistically, a million men could not find it in a year. In truth, the story of arithmetic coding is more involved than what I made it out here to be.



Figure 8: Jorma Rissanen and Stefano Zambelli at the home of K. Vela Velupillai in Galway, Ireland, March 2005.

What is your view on breadth versus depth in research? You have solved problems over a broad range and reached many deep findings. Some people tend to think that working deeply on a small topic is in contrast to having a wider interest.

I see no contradiction in the two views. I sometimes tell young people that you need mathematics and deep analytic tools if you want to accomplish anything of lasting value; you cannot do that simply by being clever in the small.

In this context I might mention a nice poem by Piet Hein, which I saw in the office door of Terry Speed in Berkeley: Its name is Wide Road and it goes as follows:

To make a name for learning when other roads are barred, take something very easy and make it very hard.

You have developed foundations of statistical modeling and carried out significant research in many fields like e.g. prediction and system theories, information and coding theory, computer learning, probability and statistics, and you have worked with computer scientists, engineers, information theorists, mathematicians, and statisticians. Could you give us your projections for statistical modeling in this new century?

In my view statistics needs a solid foundation rather than just a collection of isolated techniques however clever.

It is not enough to claim to have found a method which works well or better than other methods on some data. It's even not enough to prove that the technique works on data generated by an imagined 'true' distribution. We need to understand why a technique works as it does, and why it is better than the competing approaches. This is what's missing in current statistics,

where all sorts of criteria for the model selection problem have been proposed. In addition, a sound statistical theory should be able to treat the estimation of both the parameter values and their number within a common theory. We ought to be able to formalize ideas like 'information', 'complexity', and 'noise', which I'm afraid can be done only with information theoretic means. As a specific example, there are good techniques for denoising. However, unless the idea of 'noise' is defined it becomes the part in the data that is removed. I hope that statistics will progress in a manner which makes sense and in which the fundamental concepts are defined and the limitations clearly understood.

In many applications we are going to be faced with a lot of data generated by computational statistics or by a measuring device and then the theory has to keep up with it. Are we in a situation where there is more information than theory? Do you think there will be a revolution in statistical theory?

I already explained above that the traditional statistics is unable to formalize the central concepts that are needed to capture properties in complex data, so that indeed there is more in the data than what the traditional statistical theory can explain. In my opinion, there will be drastic changes in statistics although one may suspect that the changes will be gradual, perhaps disguised as modifications of old approaches so that no foundation need be changed. Currently, foundations, such as they are, are ignored.

Some writers seem to mix up MDL with Bayesian procedures. What is your view of the Bayesian philosophical framework?

The MDL theory is based upon the MDL principle, which opens up an entirely different approach to statistics, free from the untenable assumption of a 'true' data generating distribution, while the Bayesian philosophy has no principle other than an unrestricted use of probabilities. Instead the central concept is the posterior distribution, whose interpretation is just as fuzzy as that of the prior. Moreover, since the prior affects the posterior its selection is crucial. In the MDL theory, where the use of priors is optional, their selection must be restricted so that they are encodable. This permits optimization of their selection, which cannot be done within the Bayesian philosophy, because nothing prevents you from putting it to unity on the data. The irresistible desire to peek into the data has created concepts like 'empirical' priors which clearly contradicts the very foundation of Bayesianism.

The usual confusion between the two approaches is understandable if one equates the MDL principle with the early criterion for model selection, also derived by Bayesian arguments and called BIC. Even though they are identical the MDL derivation attaches an asymptotic optimality to the criterion, while no such status can be given to BIC in terms of the Bayesian concepts. As a result the MDL criterion has been refined and developed further, while the BIC is a dead end.

Finally, the concepts like universal models, noise, statistical information, and complexity, which are central in the MDL theory, have no meaning in the Bayesian philosophy. It is true that Bayes' formula creates a universal model, the so-called Bayesian mixture, which is good, but not because its goodness could be assessed by Bayesian means. Rather, it is good because it reaches the lower bound referred to above. Moreover, there are other universal models, which have not been found in the Bayesian philosophy and which have properties preferable to the Bayesian mixture. In summary, the MDL principle has created an entire theory with new concepts, which goes beyond any Bayesian technique and Bayesian philosophy whatever that is.

What definition of probability do you use?

Strictly speaking I use the probability that satisfies Kolmogorov's axioms. Sometimes, when it is preferable to talk about code length I mean by probability the number two raised to the negative power of the code length. After all, prefix codes are very concrete and there is nothing fuzzy about them. An example is the assignment of probability to a closed curve on the plane. It is easy to encode such curves by the chain link method, which then assigns a probability to the curve. Compare this with the horrendous task of defining a prior distribution for the set of all continuous closed curves on the plane.



Figure 9: Jorma Rissanen with Wojciech Szpankowski and Jacob Ziv at the ITA Workshop, San Diego, California, 2007.

Affiliations to Finland and current research

You were invited to "The 2nd International Tampere Conference in Statistics" in 1987. In consequence of this meeting we had the privilege to learn to know you personally. Since then you have been a regular visitor to Tampere. In 1987 Conference we had T. W. Anderson, George E. P. Box, C. R. Rao and Ted Hannan as keynote speakers. You surely had met all of them before?

I do not recall having met Professor Box before that meeting. Actually, as you may know, I met Tarmo Pukkila, who was in charge for the Tampere Conference, first time in 1985 in Las Vegas in the ASA Conference – and there Tarmo invited me to Tampere in 1987.

And now you even have a flat in Hervanta, Tampere. How do you share your time between California, Finland, and the numerous conference and lecturing trips?

I spend about two months each year in Finland on three different time periods. The conference and lecture trips do not take that much of my time.

You have been invited to numerous conferences, visited a number of universities, and have delivered many prestigious lectures, e.g. the Kolmogorov Lecture 2006. Could you mention some highlights?

In addition to the Kolmogorov lecture I remember with pleasure a talk I gave in Norbert Wiener's 100 year memorial meeting in 1994, and the visit to Ann Arbor 1986, where Shannon himself handed me the best paper award. I also remember lectures in Beijing in 2005 as a guest of Microsoft, which provided a car with the driver for a week, and a memorial meeting of Z. C. Wei in Academia Sinica in Taipei 2005.

From May 1995 until your mandatory retirement you held a part time professorship at the Tampere University of Technology. Tell us now how you came to TUT.

TUT made me an honorary doctor in 1992, which followed with a part time professorship. When I had to retire from that TUT made other special arrangements, which allowed me to visit Tampere three times each year.

Now every year you are teaching a course on statistical modeling at TUT, you are a fellow of the Helsinki Institute for Information Technology, and you have joint research projects in both places. Could you tell about these activities?

I enjoy them greatly. Now I have access to peers and graduate students, which I never had in IBM Research.

What do you want to say about your current research interests?

I'm involved in applications of the MDL principle to practical problems. I'm also involved in theoretical work, some of which has been inspired by the applications.

In addition to papers by only yourself you have plenty of papers with your collaborators. Can you shortly comment on the role of collaboration in your research?

Although I have mostly worked alone collaboration has been quite important, in particular on arithmetic coding, whose practical implementation would have been outside of my skills.

What about your PhD students? You surely must have a bunch of them?

I have had access to PhD students mostly only in Finland, and I have found them both useful and invigorating. They tend to come up with unexpected questions, which expose embarrassing shortcomings in my original suggestions. Also, of course, their superb programming skills make the applications possible, which, in turn, create further problems.

Personal

You officially had to take the mandatory retirement from your part time professorship almost ten years ago. Do you consider yourself retired?

I had no mandatory retirement from IBM Research. Rather, having already been involved in the institutions in Finland and London, I decided to retire from IBM five years ago and spend more time in Finland. I certainly do not consider myself retired. I often think that I should have retired from IBM earlier.

What things do you like to do when you are not doing research? Tell us a little bit about your life outside of research and your hobbies or other activities.

I must say that nowadays, when I don't play soccer any more, I have very little activities other than research. I walk my dog and work on the difficult to maintain yard. We live on a wild mountain side.

You have held onto your passion for soccer. Tell us what kind of resonance soccer and bandy play have had for you.

When I grew up in Kemi this game 'bandy', which is like soccer on ice with skates and a curved club to control a small ball, was my passion in winter and soccer in summer. I started to play recreational soccer in California in 1965 until my retirement in 2002. I would still play if there was an 'over 70 team' (no younger than 70 years old allowed in the team). Unfortunately, there does not seem to be enough players of that age.

As far as we remember you enjoy reading mysteries. Who are your favorite writers?

The British writers Ken Follet, Frederic Forsyth, Jack Higgins, and the Americans Clive Cussler, and Dan Brown.

You did not learn English at school? What was your way of learning your perfect English?

First, my command of English is far from perfect, but having lived in California for 40 years has helped.

What does the future hold for you?

I don't know.

Yes indeed, we don't know what the future holds. We wish you well! Thanks very much Jorma for sharing your thoughts about your career and about science with us.

I thank you for bothering to find out my thinking and making me feel as if I had done something worthwhile.



Figure 10: Jorma Rissanen looking at the sketch of a plot on sale in Kuru, Finland, April 2007.

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